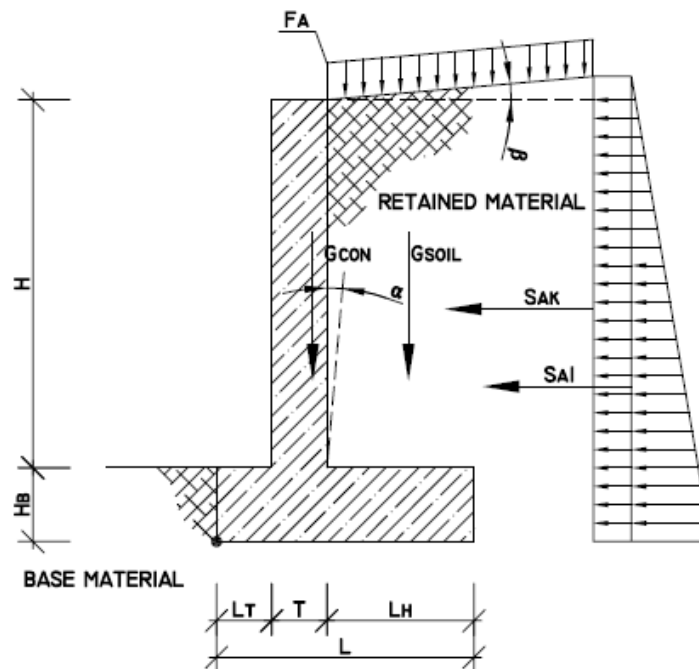


# SOFTWARE ANALYSIS OF RETAINING WALLS



Project: **Software analysis of retaining walls**

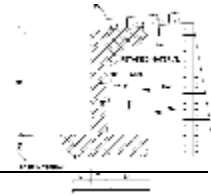
Project description: **Analysis of retaining walls of certain height made of elastoplastic concrete**

Project number: **2012014**

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Prepared for: **Elastoplastic concrete (EPC)**

Date: **October 2012**



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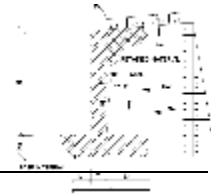
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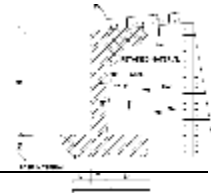


## 2. PRELUDE

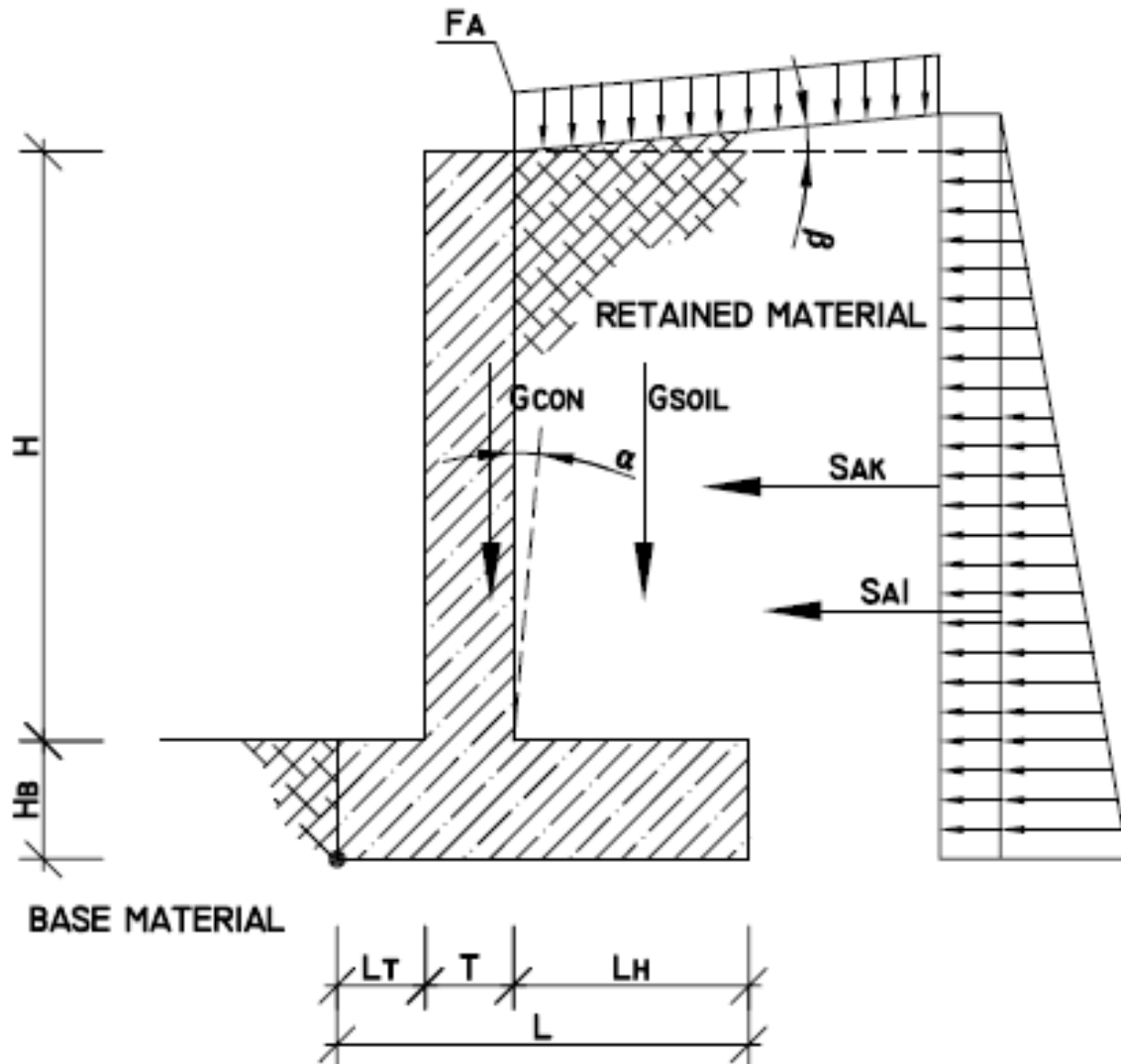
The report is written to show a possible use of elastoplastic concrete for retaining walls. The data included in the report such as the elastoplastic concrete properties have been already described in the previous reports.

This report shows the possible use for a cantilevered retaining wall of the certain height. The designed retaining walls are analysed for the all states in accordance to the Australian Standard: Earth-retaining structures – AS4678-2002: stability limit state – overturning, stability limit state – sliding, soil bearing capacity and ultimate limit state of a retaining wall.

The load used for the analysis in the report is the active earth pressure from the retained material and the passive earth pressure from the base material positively acting on an elastoplastic concrete retaining wall (no surcharge on plan and no load from water pressure). The retained material properties used for the analysis in the report is considered like one of the worst soil for this purpose. That means the analysis result is on a positive side. The base material properties used for the analysis is considered like soil with the better properties. The analysis is based on Coulomb theory which is commonly used for this sort of analyses.

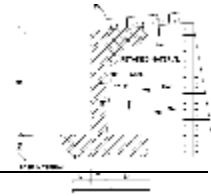


### 3. STATIC MODEL FOR ANALYSES



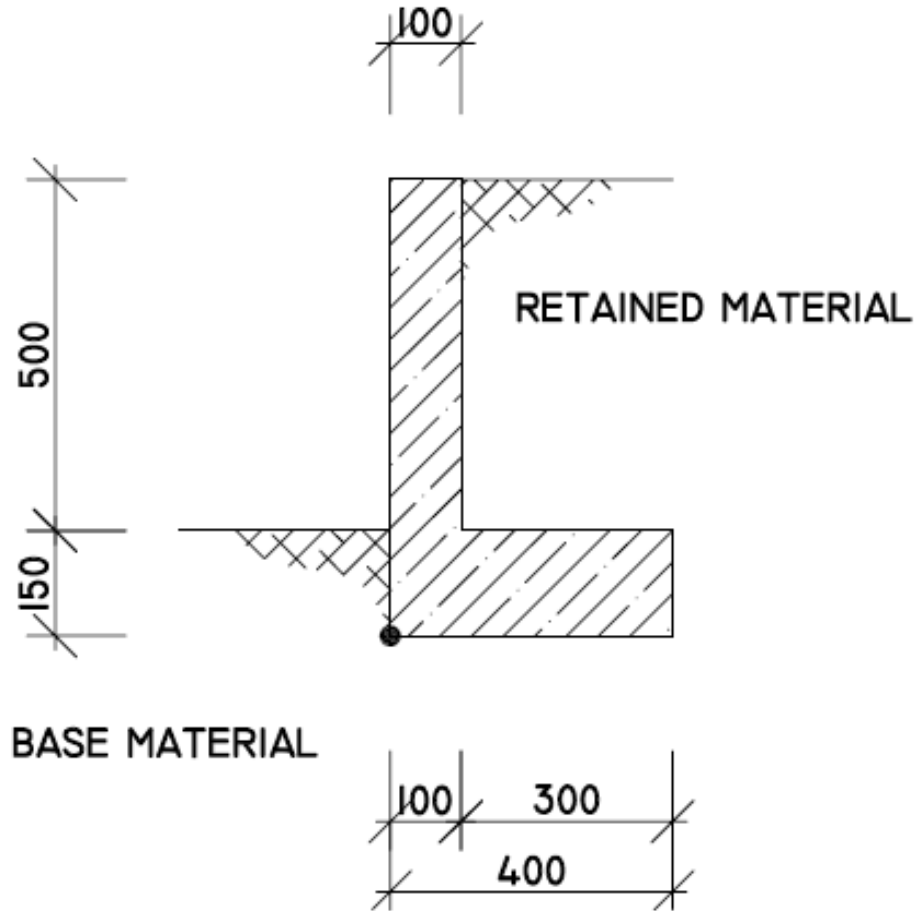
# SOFTWARE ANALYSIS OF RETAINING WALLS

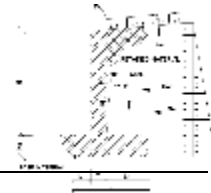
Analysis of retaining walls of  
certain height made of elastoplastic concrete



## 4. RETAINING WALL ANALYSIS (0mm - 500mm HIGH)

### 4.1 Retaining wall model





## 4.2 Retaining wall analysis

### RETAINING WAL PROPERTIES

#### **Retaining wall dimensions**

- »  $H = 0,500$  m      *Height of retaining wall stem*
- »  $H_b = 0,150$  m      *Height of retaining wall base*
- »  $h_{soil} = 0,150$  m      *Height of soil in front of the retaining wall*
- »  $l_t = 0,000$  m      *Length of toe*
- »  $t = 0,100$  m      *Retaining wall thickness*
- »  $l_h = 0,300$  m      *Length of heel*
- »  $\alpha = 0^\circ$       *Angle of rear face of wall*

#### **Extra load acting on the ground surface**

- »  $f_a = 0,00$  kN/m<sup>2</sup>      *Surcharge load on plan*
- $H_{eqv} = f_a / \gamma_{soil} = 0,000$  m      *Equivalent height of soil*

#### **Retained soil material**

- »  $\gamma_{soil} = 21,00$  kN/m<sup>3</sup>      *Density of soil*
- »  $\varphi_{ef} = 18,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85$  [-]      *Material strength uncertainty factor*
- $\varphi' = 15,44^\circ$       *Design internal friction angle*
- »  $\sigma_{Rd} = 100$  kPa      *Allowable ultimate bearing pressure*
- »  $\beta = 0^\circ$       *Angle of soil surface behind wall*
- $\delta = 10^\circ$       *Angle of base friction*

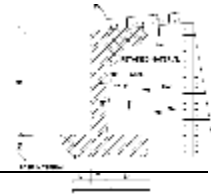
*The typical soil of this properties is claysoil.*

#### **Base soil material**

- »  $\gamma_{soil} = 19,00$  kN/m<sup>3</sup>      *Density of soil*
- »  $\varphi_{ef} = 35,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85$  [-]      *Material strength uncertainty factor*
- $\varphi' = 30,76^\circ$       *Design internal friction angle*

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of  
certain height made of elastoplastic concrete



»  $\sigma_{Rd} = 150 \text{ kPa}$       *Allowable ultimate bearing pressure*

$\delta = 21^\circ$       *Angle of base friction*

*The typical soil of this properties is gravelsoil and sand soil.*

### Concrete

» Concrete: C25/30

$f_{ck} = 25,00 \text{ MPa}$       *Characteristic compressive cylinder strength of plain concrete*

$f_{ct,f} = 3,000 \text{ MPa}$       *Characteristic flexural tensile strength of plain concrete*

»  $\gamma_{con} = 25,00 \text{ kN/m}^3$       *Density of concrete*

### Earth pressure factors

$$K_a = \frac{\cos^2(\varphi' - \alpha) \cdot [\cos^2(\alpha) \cdot \cos(\alpha + \delta) \cdot (1 + (\sin(\varphi' + \delta) \cdot \sin(\varphi' - \beta)) / (\cos(\alpha + \delta) \cdot \cos(\alpha - \beta)))^{0,5}]^2}{\cos^2(\alpha + \delta) \cdot \cos(\alpha - \beta)}$$

$K_a = 0,52$  [-]      *Active earth pressure factor*

$$K_p = [\sin(90 - \varphi')]^2 / \{ \sin(90 - \delta) \cdot [1 - ((\sin(\varphi' + \delta) \cdot \sin(\varphi') / \sin(90 + \delta))^{0,5})^2] \}$$

$K_p = 6,53$  [-]      *Passive earth pressure factor*

### A/ STABILITY ANALYSIS - OVERTURNING

$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000 \text{ kN}$       *Effective value of horizontal surcharge force*

$h_{ak} = (H_b + H) / 2 = 0,325 \text{ m}$       *Force arm of extra surcharge on plan*

$\gamma_{ak} = 1,50$  [-]      *Stability load factor for overturning live load*

$S_{a1} = (H_b + H)^2 \cdot \gamma_{soil} \cdot K_a / 2 = 2,32 \text{ kN}$       *Effective value of horizontal active earth press*

$h_{a1} = (H_b + H) / 3 = 0,217 \text{ m}$       *Force arm of active earth pressure*

$\gamma_{a1} = 1,25$  [-]      *Stability load factor for overturning dead load*

$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 2,75 \text{ kN}$       *Effective vertical force of concrete R*

$h_{con} = [(l_t + t + l_h)^2 \cdot H_b / 2 + H \cdot t \cdot (l_t + t / 2)] / [(l_t + t + l_h) \cdot H_b + H \cdot t] = 0,132 \text{ m}$       *F*

$\gamma_{con} = 0,90$  [-]      *Stability load factor for restoring dead load*

$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 3,15 \text{ kN}$       *Effective vertical force of backfill*

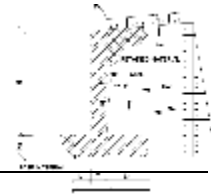
$h_{soil} = l_t + t + l_h / 3 = 0,200 \text{ m}$       *Force arm of backfill*

$\gamma_{soil} = 0,90$  [-]      *Stability load factor for restoring dead load*

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of

certain height made of elastoplastic concrete



$$M_{\text{over}} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 0,629 \text{ kNm} \quad \text{Overturning moment}$$

$$M_{\text{rest}} = G_{\text{con}} \cdot h_{\text{con}} \cdot \gamma_{\text{con}} + G_{\text{soil}} \cdot h_{\text{soil}} \cdot \gamma_{\text{soil}} = 0,89 \text{ kNm} \quad \text{Restoring moment}$$

$$M_{\text{rest}} = 0,89 \text{ kNm} > M_{\text{over}} = 0,629 \text{ kNm} \quad \text{OK}$$

### B/ ANALYSIS OF STABILITY AGAINST SLIDING

$$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$\gamma_{ak} = 1,50 \text{ [-]} \quad \text{Stability load factor for overturning live load}$$

$$S_{a1} = (H_b + H)^2 \cdot \gamma_{\text{soil}} \cdot K_a / 2 = 2,32 \text{ kN} \quad \text{Effective value of horizontal active earth press}$$

$$\gamma_{a1} = 1,25 \text{ [-]} \quad \text{Stability load factor for overturning dead load}$$

$$S_{a2} = H_{\text{soil}}^2 \cdot \gamma_{\text{soil}} \cdot K_p / 2 = 1,54 \text{ kN} \quad \text{Effective value of horizontal passive earth pressur}$$

$$\gamma_{a2} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{\text{con}} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{\text{con}} = 2,75 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{\text{con}} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{\text{soil}} = l_h \cdot H \cdot \gamma_{\text{soil}} = 3,15 \text{ kN} \quad \text{Effective vertical force of backfill}$$

$$\gamma_{\text{soil}} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$F_{\text{slid}} = S_{ak} \cdot \gamma_{ak} + S_{a1} \cdot \gamma_{a1} = 2,904 \text{ kN} \quad \text{Sliding force}$$

$$F_{\text{rest}} = \gamma_{a2} \cdot S_{a2} + (G_{\text{con}} \cdot \gamma_{\text{con}} + G_{\text{soil}} \cdot \gamma_{\text{soil}}) \cdot \text{tg } \delta = 3,375 \text{ kN} \quad \text{Resistance force}$$

$$F_{\text{rest}} = 3,38 \text{ kN} > F_{\text{slid}} = 2,90 \text{ kN} \quad \text{OK}$$

### C/ SOIL BEARING CAPACITY ANALYSIS

$$M_{\text{over}} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 0,629 \text{ kNm} \quad \text{Overturning moment}$$

$$G_{\text{con}} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{\text{con}} = 2,75 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{\text{con}} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{\text{soil}} = l_h \cdot H \cdot \gamma_{\text{soil}} = 3,15 \text{ kN} \quad \text{Effective vertical force of backfill}$$

$$\gamma_{\text{soil}} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

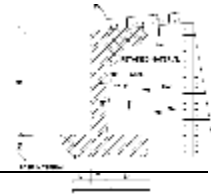
$$e = M_{\text{over}} / (\gamma_{\text{con}} \cdot G_{\text{con}} + \gamma_{\text{soil}} \cdot G_{\text{soil}}) = 0,085 \text{ m} \quad \text{Total force eccentricity}$$

$$e' = (l_t + t + l_h) / 2 - (G_{\text{con}} \cdot h_{\text{con}} + G_{\text{soil}} \cdot h_{\text{soil}}) / (G_{\text{con}} + G_{\text{soil}}) = 0,032 \text{ m}$$



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$$b_{\text{eff}} = [l_t + t + l_h - 2 \cdot (e + e')] = 0,166 \text{ m} \quad \text{Load effective width}$$

$$\sigma = (1,25 \cdot G_{\text{con}} + 1,25 \cdot G_{\text{soil}}) / b_{\text{eff}} = 44,49 \text{ kPa} \quad \text{Maximum stress in soil}$$

$$\underline{\underline{\sigma_{\text{Rd}} = 150,00 \text{ kPa} > \sigma = 44,49 \text{ kPa} \quad \text{OK}}}$$

### D/ ULTIMATE LIMIT STATE OF RETAINING WALL

#### Internal force analysis

$$S_{\text{ah}} = f_a \cdot K_a \cdot H = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$h_{\text{ah}} = H / 2 = 0,250 \text{ m} \quad \text{Force arm of horizontal surcharge force}$$

$$\gamma_{\text{ah}} = 1,50 \text{ [-]} \quad \text{Load factor for live load (ultimate limit state)}$$

$$S_{\text{a1}} = H^2 \cdot \gamma_{\text{soil}} \cdot K_a / 2 = 1,375 \text{ kN} \quad \text{Horizontal force from active earth pressure}$$

$$h_{\text{a1}} = H / 3 = 0,167 \text{ m} \quad \text{Force arm of active earth pressure}$$

$$\gamma_{\text{a1}} = 1,25 \text{ [-]} \quad \text{Load factor for dead load (ultimate limit state)}$$

$$\underline{\underline{M_{\text{Sd}} = \gamma_{\text{ah}} \cdot S_{\text{ah}} \cdot h_{\text{ah}} + \gamma_{\text{a1}} \cdot S_{\text{a1}} \cdot h_{\text{a1}} = 0,29 \text{ kNm} \quad \text{Design bending moment}}}$$

#### Fiber concrete structure analysis

$$b = 1,000 \text{ m} \quad \text{Width of a cross-section}$$

$$h = 0,100 \text{ m} \quad \text{Height of a cross-section}$$

$$f_{\text{ck}} = 25,00 \text{ MPa} \quad \text{Characteristic compressive cylinder strength of plain concrete}$$

$$f_{\text{ct,f}} = 3,000 \text{ MPa} \quad \text{Characteristic flexural tensile strength of plain concrete}$$

$$\phi = 0,60 \quad \text{Capacity reduction factor}$$

#### Elastoplastic concrete properties

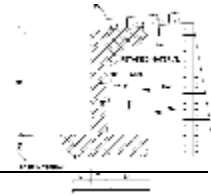
$$\underline{\underline{m_f = 2,50 \text{ kg/m}^3}} \quad \text{Dosage of plastic fibres per m}^3 \text{ (max. 7,5 kg)}$$

$$f_{\text{ct,f}} = 3,356 \text{ MPa} \quad \text{Characteristic flexural tensile strength of fiberconcrete}$$

$$I_y = b \cdot h^3 / 12 = 8,33\text{E-}05 \text{ m}^4 \quad \text{Second moment of area of the cross-section}$$

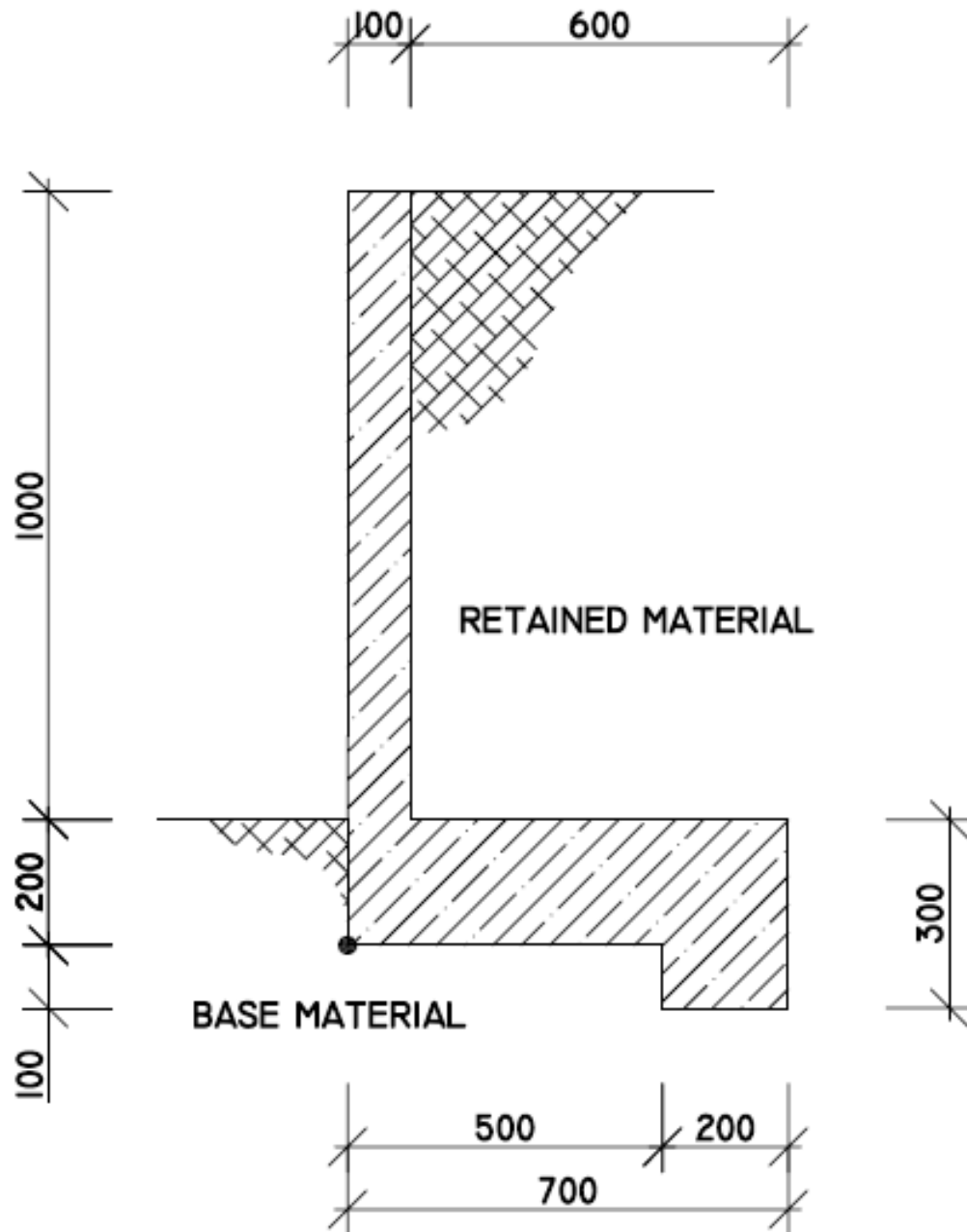
$$\underline{\underline{M_{\text{uo}} = 1,2 \cdot f_{\text{ct,f}} \cdot I_y / (h / 2) \cdot \Phi = 4,028 \text{ kNm} \quad \text{Design strength in bending}}}$$

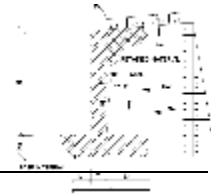
$$\underline{\underline{M_{\text{uo}} = 4,028 \text{ kNm} > M_{\text{Sd}} = 0,286 \text{ kNm} \quad \text{OK}}}$$



## 5. RETAINING WALL ANALYSIS (0mm - 1000mm HIGH)

### 5.1 Retaining wall model





## 5.2 Retaining wall analysis

### RETAINING WAL PROPERTIES

#### **Retaining wall dimensions**

- »  $H = 1,000 \text{ m}$       *Height of retaining wall stem*
- »  $H_b = 0,200 \text{ m}$       *Height of retaining wall base*
- »  $h_{\text{soil}} = 0,300 \text{ m}$       *Height of soil in front of the retaining wall*
- »  $l_t = 0,000 \text{ m}$       *Length of toe*
- »  $t = 0,100 \text{ m}$       *Retaining wall thickness*
- »  $l_h = 0,600 \text{ m}$       *Length of heel*
- »  $\alpha = 0^\circ$       *Angle of rear face of wall*

#### **Extra load acting on the ground surface**

- »  $f_a = 0,00 \text{ kN/m}^2$       *Surcharge load on plan*
- »  $H_{\text{eqv}} = f_a / \gamma_{\text{soil}} = 0,000 \text{ m}$       *Equivalent height of soil*

#### **Retained soil material**

- »  $\gamma_{\text{soil}} = 21,00 \text{ kN/m}^3$       *Density of soil*
- »  $\varphi_{\text{ef}} = 18,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85 [-]$       *Material strength uncertainty factor*
- »  $\varphi' = 15,44^\circ$       *Design internal friction angle*
- »  $\sigma_{\text{Rd}} = 100 \text{ kPa}$       *Allowable ultimate bearing pressure*
- »  $\beta = 0^\circ$       *Angle of soil surface behind wall*
- »  $\delta = 10^\circ$       *Angle of base friction*

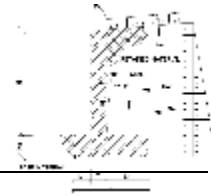
*The typical soil of this properties is claysoil.*

#### **Base soil material**

- »  $\gamma_{\text{soil}} = 19,00 \text{ kN/m}^3$       *Density of soil*
- »  $\varphi_{\text{ef}} = 35,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85 [-]$       *Material strength uncertainty factor*
- »  $\varphi' = 30,76^\circ$       *Design internal friction angle*

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»  $\sigma_{Rd} = 150 \text{ kPa}$       *Allowable ultimate bearing pressure*

$\delta = 21^\circ$       *Angle of base friction*

*The typical soil of this properties is gravelsoil and sand soil.*

### Concrete

» Concrete: C25/30

$f_{ck} = 25,00 \text{ MPa}$       *Characteristic compressive cylinder strength of plain concrete*

$f_{ct,f} = 3,000 \text{ MPa}$       *Characteristic flexural tensile strength of plain concrete*

»  $\gamma_{con} = 25,00 \text{ kN/m}^3$       *Density of concrete*

### Earth pressure factors

$$K_a = \frac{\cos^2(\varphi' - \alpha) \cdot [\cos^2(\alpha) \cdot \cos(\alpha + \delta) \cdot (1 + (\sin(\varphi' + \delta) \cdot \sin(\varphi' - \beta)) / (\cos(\alpha + \delta) \cdot \cos(\alpha - \beta)))^{0,5}]^2}{\cos^2(\alpha + \delta) \cdot \cos(\alpha - \beta)}$$

$K_a = 0,52 \text{ [-]}$       *Active earth pressure factor*

$$K_p = [\sin(90 - \varphi')^2 / \{\sin(90 - \delta) \cdot [1 - ((\sin(\varphi' + \delta) \cdot \sin(\varphi') / \sin(90 + \delta))^{0,5}]^2\}]$$

$K_p = 6,53 \text{ [-]}$       *Passive earth pressure factor*

## A/ STABILITY ANALYSIS

$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000 \text{ kN}$       *Effective value of horizontal surcharge force*

$h_{ak} = (H_b + H) / 2 = 0,600 \text{ m}$       *Force arm of extra surcharge on plan*

$\gamma_{ak} = 1,50 \text{ [-]}$       *Stability load factor for overturning live load*

$S_{a1} = (H_b + H)^2 \cdot \gamma_{soil} \cdot K_a / 2 = 7,92 \text{ kN}$       *Effective value of horizontal active earth press*

$h_{a1} = (H_b + H) / 3 = 0,400 \text{ m}$       *Force arm of active earth pressure*

$\gamma_{a1} = 1,25 \text{ [-]}$       *Stability load factor for overturning dead load*

$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 6,00 \text{ kN}$       *Effective vertical force of concrete R*

$h_{con} = [(l_t + t + l_h)^2 \cdot H_b / 2 + H \cdot t \cdot (l_t + t / 2)] / [(l_t + t + l_h) \cdot H_b + H \cdot t] = 0,225 \text{ m}$       *F*

$\gamma_{con} = 0,90 \text{ [-]}$       *Stability load factor for restoring dead load*

$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 12,60 \text{ kN}$       *Effective vertical force of backfill*

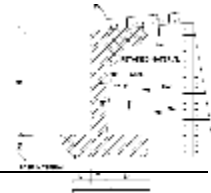
$h_{soil} = l_t + t + l_h / 3 = 0,300 \text{ m}$       *Force arm of backfill*

$\gamma_{soil} = 0,90 \text{ [-]}$       *Stability load factor for restoring dead load*

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$$M_{\text{over}} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 3,960 \text{ kNm} \quad \text{Overturning moment}$$

$$M_{\text{rest}} = G_{\text{con}} \cdot h_{\text{con}} \cdot \gamma_{\text{con}} + G_{\text{soil}} \cdot h_{\text{soil}} \cdot \gamma_{\text{soil}} = 4,62 \text{ kNm} \quad \text{Restoring moment}$$

$$M_{\text{rest}} = 4,62 \text{ kNm} > M_{\text{over}} = 3,960 \text{ kNm} \quad \text{OK}$$

### B/ ANALYSIS OF STABILITY AGAINST SLIDING

$$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$\gamma_{ak} = 1,50 \text{ [-]} \quad \text{Stability load factor for overturning live load}$$

$$S_{a1} = (H_b + H)^2 \cdot \gamma_{\text{soil}} \cdot K_a / 2 = 7,92 \text{ kN} \quad \text{Effective value of horizontal active earth pressure}$$

$$\gamma_{a1} = 1,25 \text{ [-]} \quad \text{Stability load factor for overturning dead load}$$

$$S_{a2} = H_{\text{soil}}^2 \cdot \gamma_{\text{soil}} \cdot K_p / 2 = 6,18 \text{ kN} \quad \text{Effective value of horizontal passive earth pressure}$$

$$\gamma_{a2} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{\text{con}} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{\text{con}} = 6,00 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{\text{con}} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{\text{soil}} = l_h \cdot H \cdot \gamma_{\text{soil}} = 12,60 \text{ kN} \quad \text{Effective vertical force of backfill}$$

$$\gamma_{\text{soil}} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$F_{\text{slid}} = S_{ak} \cdot \gamma_{ak} + S_{a1} \cdot \gamma_{a1} = 9,899 \text{ kN} \quad \text{Sliding force}$$

$$F_{\text{rest}} = \gamma_{a2} \cdot S_{a2} + (G_{\text{con}} \cdot \gamma_{\text{con}} + G_{\text{soil}} \cdot \gamma_{\text{soil}}) \cdot \text{tg } \delta = 11,82 \text{ kN} \quad \text{Resistance force}$$

$$F_{\text{rest}} = 11,82 \text{ kN} > F_{\text{slid}} = 9,90 \text{ kN} \quad \text{OK}$$

### C/ SOIL BEARING CAPACITY ANALYSIS

$$M_{\text{over}} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 3,960 \text{ kNm} \quad \text{Overturning moment}$$

$$G_{\text{con}} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{\text{con}} = 6,00 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{\text{con}} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{\text{soil}} = l_h \cdot H \cdot \gamma_{\text{soil}} = 12,60 \text{ kN} \quad \text{Effective vertical force of backfill}$$

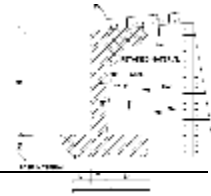
$$\gamma_{\text{soil}} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$e = M_{\text{over}} / (\gamma_{\text{con}} \cdot G_{\text{con}} + \gamma_{\text{soil}} \cdot G_{\text{soil}}) = 0,170 \text{ m} \quad \text{Total force eccentricity}$$

$$e' = (l_t + t + l_h) / 2 - (G_{\text{con}} \cdot h_{\text{con}} + G_{\text{soil}} \cdot h_{\text{soil}}) / (G_{\text{con}} + G_{\text{soil}}) = 0,074 \text{ m}$$

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of  
certain height made of elastoplastic concrete



$$b_{\text{eff}} = [l_t + t + l_h - 2 \cdot (e + e')] = 0,211 \text{ m} \quad \text{Load effective width}$$

$$\sigma = (1,25 \cdot G_{\text{con}} + 1,25 \cdot G_{\text{soil}}) / b_{\text{eff}} = 110,19 \text{ kPa} \quad \text{Maximum stress in soil}$$

$$\underline{\underline{\sigma_{\text{Rd}} = 150,00 \text{ kPa} > \sigma = 110,19 \text{ kPa} \quad \text{OK}}}$$

### D/ ULTIMATE LIMIT STATE OF RETAINING WALL

#### Internal force analysis

$$S_{\text{ah}} = f_a \cdot K_a \cdot H = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$h_{\text{ah}} = H / 2 = 0,500 \text{ m} \quad \text{Force arm of horizontal surcharge force}$$

$$\gamma_{\text{ah}} = 1,50 \text{ [-]} \quad \text{Load factor for live load (ultimate limit state)}$$

$$S_{\text{a1}} = H^2 \cdot \gamma_{\text{soil}} \cdot K_a / 2 = 5,500 \text{ kN} \quad \text{Horizontal force from active earth pressure}$$

$$h_{\text{a1}} = H / 3 = 0,333 \text{ m} \quad \text{Force arm of active earth pressure}$$

$$\gamma_{\text{a1}} = 1,25 \text{ [-]} \quad \text{Load factor for dead load (ultimate limit state)}$$

$$\underline{\underline{M_{\text{Sd}} = \gamma_{\text{ah}} \cdot S_{\text{ah}} \cdot h_{\text{ah}} + \gamma_{\text{a1}} \cdot S_{\text{a1}} \cdot h_{\text{a1}} = 2,29 \text{ kNm} \quad \text{Design bending moment}}}$$

#### Fiber concrete structure analysis

$$b = 1,000 \text{ m} \quad \text{Width of a cross-section}$$

$$h = 0,100 \text{ m} \quad \text{Height of a cross-section}$$

$$f_{\text{ck}} = 25,00 \text{ MPa} \quad \text{Characteristic compressive cylinder strength of plain concrete}$$

$$f_{\text{ct,f}} = 3,000 \text{ MPa} \quad \text{Characteristic flexural tensile strength of plain concrete}$$

$$\phi = 0,60 \quad \text{Capacity reduction factor}$$

#### Elastoplastic concrete properties

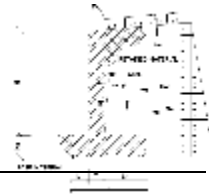
$$\underline{\underline{m_f = 2,50 \text{ kg/m}^3}} \quad \text{Dosage of plastic fibres per m}^3 \text{ (max. 7,5 kg)}$$

$$f_{\text{ct,f}} = 3,356 \text{ MPa} \quad \text{Characteristic flexural tensile strength of fiberconcrete}$$

$$I_y = b \cdot h^3 / 12 = 8,33\text{E-}05 \text{ m}^4 \quad \text{Second moment of area of the cross-section}$$

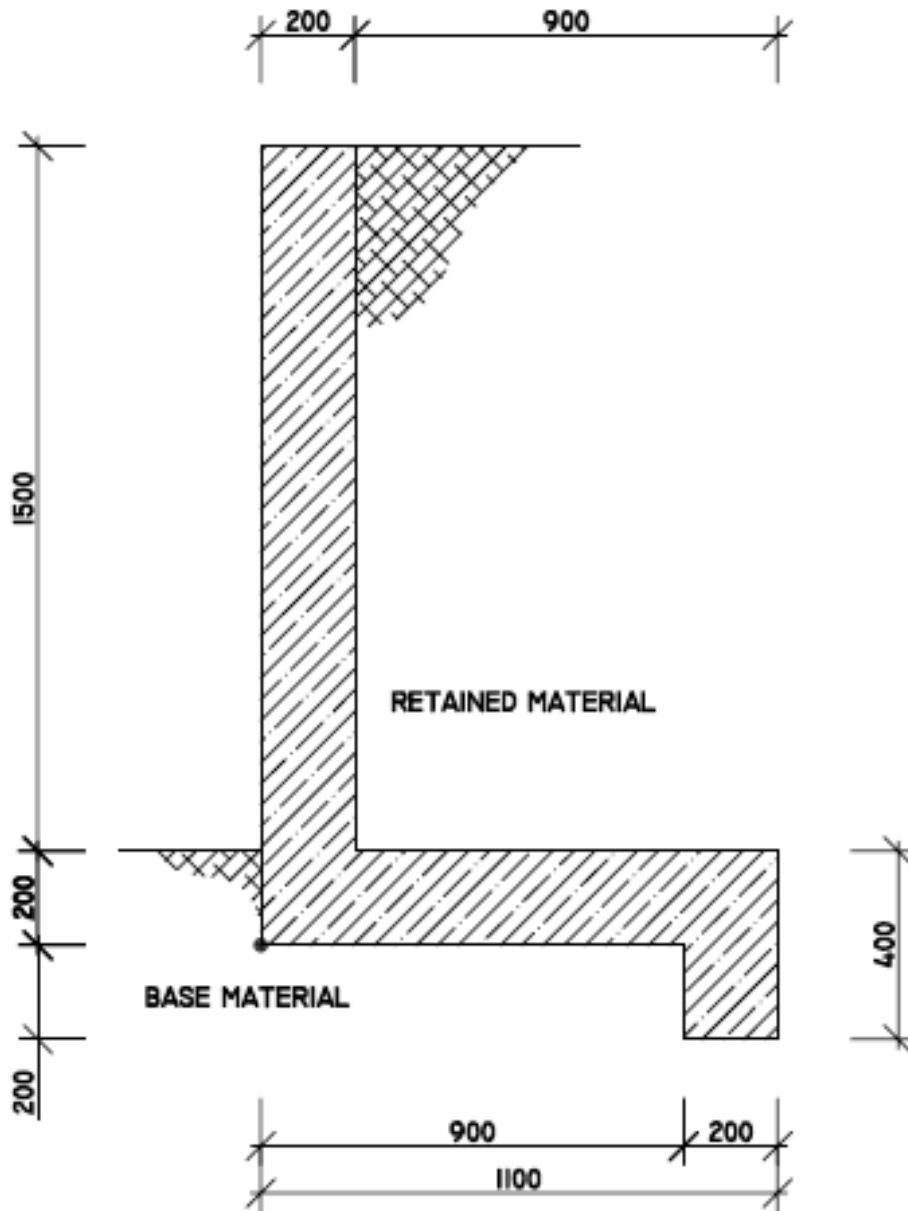
$$\underline{\underline{M_{\text{uo}} = 1,2 \cdot f_{\text{ct,f}} \cdot I_y / (h / 2) \cdot \Phi = 4,028 \text{ kNm} \quad \text{Design strength in bending}}}$$

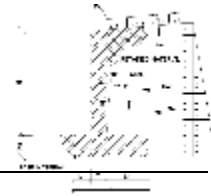
$$\underline{\underline{M_{\text{uo}} = 4,028 \text{ kNm} > M_{\text{Sd}} = 2,291 \text{ kNm} \quad \text{OK}}}$$



## 6. RETAINING WALL ANALYSIS (0mm - 1500mm HIGH)

### 6.1 Retaining wall model





## 6.2 Retaining wall model

### RETAINING WAL PROPERTIES

#### Retaining wall dimensions

- »  $H = 1,500$  m      *Height of retaining wall stem*
- »  $H_b = 0,200$  m      *Height of retaining wall base*
- »  $h_{soil} = 0,400$  m      *Height of soil in front of the retaining wall*
- »  $l_t = 0,000$  m      *Length of toe*
- »  $t = 0,200$  m      *Retaining wall thickness*
- »  $l_h = 0,900$  m      *Length of heel*
- »  $\alpha = 0^\circ$       *Angle of rear face of wall*

#### Extra load acting on the ground surface

- »  $f_a = 0,00$  kN/m<sup>2</sup>      *Surcharge load on plan*
- $H_{eqv} = f_a / \gamma_{soil} = 0,000$  m      *Equivalent height of soil*

#### Retained soil material

- »  $\gamma_{soil} = 21,00$  kN/m<sup>3</sup>      *Density of soil*
- »  $\varphi_{ef} = 18,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85$  [-]      *Material strength uncertainty factor*
- $\varphi' = 15,44^\circ$       *Design internal friction angle*
- »  $\sigma_{Rd} = 100$  kPa      *Allowable ultimate bearing pressure*
- »  $\beta = 0^\circ$       *Angle of soil surface behind wall*
- $\delta = 10^\circ$       *Angle of base friction*

*The typical soil of this properties is claysoil.*

#### Base soil material

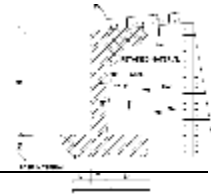
- »  $\gamma_{soil} = 19,00$  kN/m<sup>3</sup>      *Density of soil*
- »  $\varphi_{ef} = 35,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85$  [-]      *Material strength uncertainty factor*
- $\varphi' = 30,76^\circ$       *Design internal friction angle*
- »  $\sigma_{Rd} = 150$  kPa      *Allowable ultimate bearing pressure*
- $\delta = 21^\circ$       *Angle of base friction*

*The typical soil of this properties is gravelsoil and sand soil.*



## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of  
certain height made of elastoplastic concrete



### Concrete

» Concrete: C25/30

$f_{ck} = 25,00$  MPa      *Characteristic compressive cylinder strength of plain concrete*

$f_{ct,f} = 3,000$  MPa      *Characteristic flexural tensile strength of plain concrete*

»  $\gamma_{con} = 25,00$  kN/m<sup>3</sup>      *Density of concrete*

### Earth pressure factors

$$K_a = \cos^2(\varphi' - \alpha) / [\cos^2(\alpha) \cdot \cos(\alpha + \delta) \cdot (1 + (\sin(\varphi' + \delta) \cdot \sin(\varphi' - \beta)) / (\cos(\alpha + \delta) \cdot \cos(\alpha - \beta)))^{0,5}]^2$$

$K_a = 0,52$  [-]      *Active earth pressure factor*

$$K_p = [\sin(90 - \varphi')]^2 / \{ \sin(90 - \delta) \cdot [1 - ((\sin(\varphi' + \delta) \cdot \sin(\varphi') / \sin(90 + \delta))^{0,5})^2] \}$$

$K_p = 6,53$  [-]      *Passive earth pressure factor*

### A/ STABILITY ANALYSIS - OVERTURNING

$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000$  kN      *Effective value of horizontal surcharge force*

$h_{ak} = (H_b + H) / 2 = 0,850$  m      *Force arm of extra surcharge on plan*

$\gamma_{ak} = 1,50$  [-]      *Stability load factor for overturning live load*

$S_{a1} = (H_b + H)^2 \cdot \gamma_{soil} \cdot K_a / 2 = 15,9$  kN      *Effective value of horizontal active earth press*

$h_{a1} = (H_b + H) / 3 = 0,567$  m      *Force arm of active earth pressure*

$\gamma_{a1} = 1,25$  [-]      *Stability load factor for overturning dead load*

$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 13,00$  kN      *Effective vertical force of concrete R*

$h_{con} = [(l_t + t + l_h)^2 \cdot H_b / 2 + H \cdot t \cdot (l_t + t / 2)] / [(l_t + t + l_h) \cdot H_b + H \cdot t] = 0,290$  m      *F*

$\gamma_{con} = 0,90$  [-]      *Stability load factor for restoring dead load*

$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 28,35$  kN      *Effective vertical force of backfill*

$h_{soil} = l_t + t + l_h / 3 = 0,500$  m      *Force arm of backfill*

$\gamma_{soil} = 0,90$  [-]      *Stability load factor for restoring dead load*

$M_{over} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 11,26$  kNm      *Overturning moment*

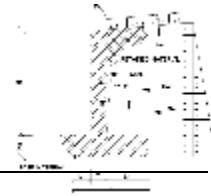
$M_{rest} = G_{con} \cdot h_{con} \cdot \gamma_{con} + G_{soil} \cdot h_{soil} \cdot \gamma_{soil} = 16,16$  kNm      *Restoring moment*

$M_{rest} = 16,16$  kNm >  $M_{over} = 11,26$  kNm      **OK**

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of

certain height made of elastoplastic concrete



### B/ ANALYSIS OF STABILITY AGAINST SLIDING

$$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$\gamma_{ak} = 1,50 \text{ [-]} \quad \text{Stability load factor for overturning live load}$$

$$S_{a1} = (H_b + H)^2 \cdot \gamma_{soil} \cdot K_a / 2 = 15,9 \text{ kN} \quad \text{Effective value of horizontal active earth press}$$

$$\gamma_{a1} = 1,25 \text{ [-]} \quad \text{Stability load factor for overturning dead load}$$

$$S_{a2} = H_{soil}^2 \cdot \gamma_{soil} \cdot K_p / 2 = 11,0 \text{ kN} \quad \text{Effective value of horizontal passive earth pressur}$$

$$\gamma_{a2} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 13,00 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{con} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 28,35 \text{ kN} \quad \text{Effective vertical force of backfill}$$

$$\gamma_{soil} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$F_{slid} = S_{ak} \cdot \gamma_{ak} + S_{a1} \cdot \gamma_{a1} = 19,87 \text{ kN} \quad \text{Sliding force}$$

$$F_{rest} = \gamma_{a2} \cdot S_{a2} + (G_{con} \cdot \gamma_{con} + G_{soil} \cdot \gamma_{soil}) \cdot \text{tg } \delta = 23,80 \text{ kN} \quad \text{Resistance force}$$

$$F_{rest} = 23,80 \text{ kN} > F_{slid} = 19,87 \text{ kN} \quad \text{OK}$$

### C/ SOIL BEARING CAPACITY ANALYSIS

$$M_{over} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 11,26 \text{ kNm} \quad \text{Overturning moment}$$

$$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 13,00 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{con} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 28,35 \text{ kN} \quad \text{Effective vertical force of backfill}$$

$$\gamma_{soil} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$e = M_{over} / (\gamma_{con} \cdot G_{con} + \gamma_{soil} \cdot G_{soil}) = 0,218 \text{ m} \quad \text{Total force eccentricity}$$

$$e' = (l_t + t + l_h) / 2 - (G_{con} \cdot h_{con} + G_{soil} \cdot h_{soil}) / (G_{con} + G_{soil}) = 0,116 \text{ m}$$

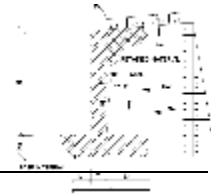
$$b_{eff} = [l_t + t + l_h - 2 \cdot (e + e')] = 0,433 \text{ m} \quad \text{Load effective width}$$

$$\sigma = (1,25 \cdot G_{con} + 1,25 \cdot G_{soil}) / b_{eff} = 119,49 \text{ kPa} \quad \text{Maximum stress in soil}$$

$$\sigma_{Rd} = 150,00 \text{ kPa} > \sigma = 119,49 \text{ kPa} \quad \text{OK}$$

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of  
certain height made of elastoplastic concrete



### D/ ULTIMATE LIMIT STATE OF RETAINING WALL

#### Internal force analysis

$$S_{ah} = f_a \cdot K_a \cdot H = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$h_{ah} = H / 2 = 0,750 \text{ m} \quad \text{Force arm of horizontal surcharge force}$$

$$\gamma_{ah} = 1,50 \text{ [-]} \quad \text{Load factor for live load (ultimate limit state)}$$

$$S_{a1} = H^2 \cdot \gamma_{soil} \cdot K_a / 2 = 12,37 \text{ kN} \quad \text{Horizontal force from active earth pressure}$$

$$h_{a1} = H / 3 = 0,500 \text{ m} \quad \text{Force arm of active earth pressure}$$

$$\gamma_{a1} = 1,25 \text{ [-]} \quad \text{Load factor for dead load (ultimate limit state)}$$

$$M_{Sd} = \gamma_{ah} \cdot S_{ah} \cdot h_{ah} + \gamma_{a1} \cdot S_{a1} \cdot h_{a1} = 7,73 \text{ kNm} \quad \text{Design bending moment}$$

#### Fiber concrete structure analysis

$$b = 1,000 \text{ m} \quad \text{Width of a cross-section}$$

$$h = 0,200 \text{ m} \quad \text{Height of a cross-section}$$

$$f_{ck} = 25,00 \text{ MPa} \quad \text{Characteristic compressive cylinder strength of plain concrete}$$

$$f_{ct,f} = 3,000 \text{ MPa} \quad \text{Characteristic flexural tensile strength of plain concrete}$$

$$\phi = 0,60 \quad \text{Capacity reduction factor}$$

#### Elastoplastic concrete properties

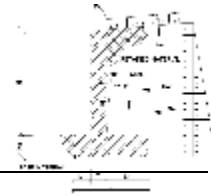
$$m_f = 2,50 \text{ kg/m}^3 \quad \text{Dosage of plastic fibres per m}^3 \text{ (max. 7,5 kg)}$$

$$f_{ict,f} = 3,356 \text{ MPa} \quad \text{Characteristic flexural tensile strength of fiberconcrete}$$

$$I_y = b \cdot h^3 / 12 = 0,000667 \text{ m}^4 \quad \text{Second moment of area of the cross-section}$$

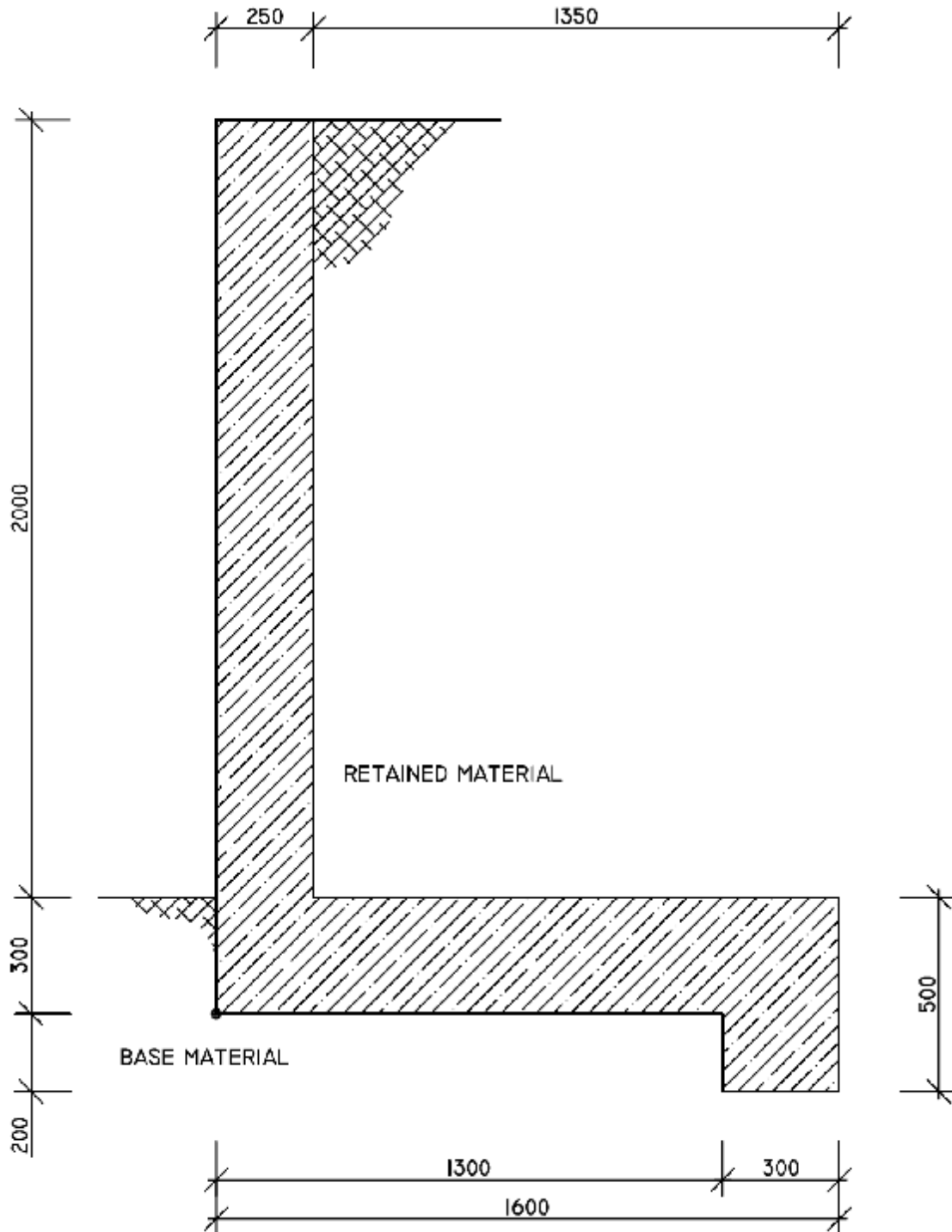
$$M_{uo} = 1,2 \cdot f_{ict,f} \cdot I_y / (h / 2) \cdot \Phi = 16,110 \text{ kNm} \quad \text{Design strength in bending}$$

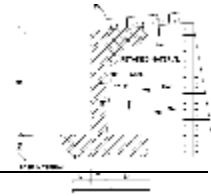
$$M_{uo} = 16,11 \text{ kNm} > M_{Sd} = 7,734 \text{ kNm} \quad \text{OK}$$



## 7. RETAINING WALL ANALYSIS (0mm - 2000mm HIGH)

### 7.1 Retaining wall model





## 7.2 Retaining wall model

### RETAINING WAL PROPERTIES

#### Retaining wall dimensions

- »  $H = 2,000 \text{ m}$       *Height of retaining wall stem*
- »  $H_b = 0,300 \text{ m}$       *Height of retaining wall base*
- »  $h_{\text{soil}} = 0,500 \text{ m}$       *Height of soil in front of the retaining wall*
- »  $l_t = 0,000 \text{ m}$       *Length of toe*
- »  $t = 0,250 \text{ m}$       *Retaining wall thickness*
- »  $l_h = 1,350 \text{ m}$       *Length of heel*
- »  $\alpha = 0^\circ$       *Angle of rear face of wall*

#### Extra load acting on the ground surface

- »  $f_a = 0,00 \text{ kN/m}^2$       *Surcharge load on plan*
- »  $H_{\text{eqv}} = f_a / \gamma_{\text{soil}} = 0,000 \text{ m}$       *Equivalent height of soil*

#### Retained soil material

- »  $\gamma_{\text{soil}} = 21,00 \text{ kN/m}^3$       *Density of soil*
- »  $\varphi_{\text{ef}} = 18,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85$  [-]      *Material strength uncertainty factor*
- »  $\varphi' = 15,44^\circ$       *Design internal friction angle*
- »  $\sigma_{\text{Rd}} = 100 \text{ kPa}$       *Allowable ultimate bearing pressure*
- »  $\beta = 0^\circ$       *Angle of soil surface behind wall*
- »  $\delta = 10^\circ$       *Angle of base friction*

*The typical soil of this properties is claysoil.*

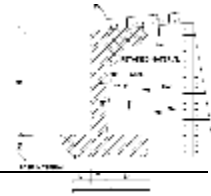
#### Base soil material

- »  $\gamma_{\text{soil}} = 19,00 \text{ kN/m}^3$       *Density of soil*
- »  $\varphi_{\text{ef}} = 35,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85$  [-]      *Material strength uncertainty factor*
- »  $\varphi' = 30,76^\circ$       *Design internal friction angle*
- »  $\sigma_{\text{Rd}} = 150 \text{ kPa}$       *Allowable ultimate bearing pressure*
- »  $\delta = 21^\circ$       *Angle of base friction*

*The typical soil of this properties is gravelsoil and sand soil.*

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of  
certain height made of elastoplastic concrete



### Concrete

» Concrete: C25/30

$f_{ck} = 25,00$  MPa      *Characteristic compressive cylinder strength of plain concrete*

$f_{ct,f} = 3,000$  MPa      *Characteristic flexural tensile strength of plain concrete*

»  $\gamma_{con} = 25,00$  kN/m<sup>3</sup>      *Density of concrete*

### Earth pressure factors

$$K_a = \cos^2(\varphi' - \alpha) / [\cos^2(\alpha) \cdot \cos(\alpha + \delta) \cdot (1 + (\sin(\varphi' + \delta) \cdot \sin(\varphi' - \beta)) / (\cos(\alpha + \delta) \cdot \cos(\alpha - \beta)))^{0,5}]^2$$

$K_a = 0,52$  [-]      *Active earth pressure factor*

$$K_p = [\sin(90 - \varphi')]^2 / \{ \sin(90 - \delta) \cdot [1 - ((\sin(\varphi' + \delta) \cdot \sin(\varphi') / \sin(90 + \delta))^{0,5})^2] \}$$

$K_p = 6,53$  [-]      *Passive earth pressure factor*

### A/ STABILITY ANALYSIS - OVERTURNING

$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000$  kN      *Effective value of horizontal surcharge force*

$h_{ak} = (H_b + H) / 2 = 1,150$  m      *Force arm of extra surcharge on plan*

$\gamma_{ak} = 1,50$  [-]      *Stability load factor for overturning live load*

$S_{a1} = (H_b + H)^2 \cdot \gamma_{soil} \cdot K_a / 2 = 29,1$  kN      *Effective value of horizontal active earth press*

$h_{a1} = (H_b + H) / 3 = 0,767$  m      *Force arm of active earth pressure*

$\gamma_{a1} = 1,25$  [-]      *Stability load factor for overturning dead load*

$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 24,50$  kN      *Effective vertical force of concrete R*

$h_{con} = [(l_t + t + l_h)^2 \cdot H_b / 2 + H \cdot t \cdot (l_t + t / 2)] / [(l_t + t + l_h) \cdot H_b + H \cdot t] = 0,456$  m      *F*

$\gamma_{con} = 0,90$  [-]      *Stability load factor for restoring dead load*

$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 56,70$  kN      *Effective vertical force of backfill*

$h_{soil} = l_t + t + l_h / 3 = 0,700$  m      *Force arm of backfill*

$\gamma_{soil} = 0,90$  [-]      *Stability load factor for restoring dead load*

$M_{over} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 27,88$  kNm      *Overturning moment*

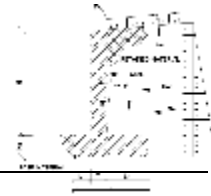
$M_{rest} = G_{con} \cdot h_{con} \cdot \gamma_{con} + G_{soil} \cdot h_{soil} \cdot \gamma_{soil} = 45,77$  kNm      *Restoring moment*

$M_{rest} = 45,77$  kNm >  $M_{over} = 27,88$  kNm OK

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of

certain height made of elastoplastic concrete



### B/ ANALYSIS OF STABILITY AGAINST SLIDING

$$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$\gamma_{ak} = 1,50 \text{ [-]} \quad \text{Stability load factor for overturning live load}$$

$$S_{a1} = (H_b + H)^2 \cdot \gamma_{soil} \cdot K_a / 2 = 29,1 \text{ kN} \quad \text{Effective value of horizontal active earth press}$$

$$\gamma_{a1} = 1,25 \text{ [-]} \quad \text{Stability load factor for overturning dead load}$$

$$S_{a2} = H_{soil}^2 \cdot \gamma_{soil} \cdot K_p / 2 = 17,2 \text{ kN} \quad \text{Effective value of horizontal passive earth pressur}$$

$$\gamma_{a2} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 24,50 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{con} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 56,70 \text{ kN} \quad \text{Effective vertical force of backfill}$$

$$\gamma_{soil} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$F_{slid} = S_{ak} \cdot \gamma_{ak} + S_{a1} \cdot \gamma_{a1} = 36,37 \text{ kN} \quad \text{Sliding force}$$

$$F_{rest} = \gamma_{a2} \cdot S_{a2} + (G_{con} \cdot \gamma_{con} + G_{soil} \cdot \gamma_{soil}) \cdot \text{tg } \delta = 42,77 \text{ kN} \quad \text{Resistance force}$$

$$F_{rest} = 42,77 \text{ kN} > F_{slid} = 36,37 \text{ kN} \quad \text{OK}$$

### C/ SOIL BEARING CAPACITY ANALYSIS

$$M_{over} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 27,88 \text{ kNm} \quad \text{Overturning moment}$$

$$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 24,50 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{con} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 56,70 \text{ kN} \quad \text{Effective vertical force of backfill}$$

$$\gamma_{soil} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$e = M_{over} / (\gamma_{con} \cdot G_{con} + \gamma_{soil} \cdot G_{soil}) = 0,275 \text{ m} \quad \text{Total force eccentricity}$$

$$e' = (l_t + t + l_h) / 2 - (G_{con} \cdot h_{con} + G_{soil} \cdot h_{soil}) / (G_{con} + G_{soil}) = 0,174 \text{ m}$$

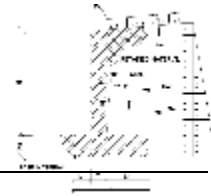
$$b_{eff} = [l_t + t + l_h - 2 \cdot (e + e')] = 0,703 \text{ m} \quad \text{Load effective width}$$

$$\sigma = (1,25 \cdot G_{con} + 1,25 \cdot G_{soil}) / b_{eff} = 144,35 \text{ kPa} \quad \text{Maximum stress in soil}$$

$$\sigma_{Rd} = 150,00 \text{ kPa} > \sigma = 144,35 \text{ kPa} \quad \text{OK}$$

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of  
certain height made of elastoplastic concrete



### D/ ULTIMATE LIMIT STATE OF RETAINING WALL

#### Internal force analysis

$$S_{ah} = f_a \cdot K_a \cdot H = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$h_{ah} = H / 2 = 1,000 \text{ m} \quad \text{Force arm of horizontal surcharge force}$$

$$\gamma_{ah} = 1,50 \text{ [-]} \quad \text{Load factor for live load (ultimate limit state)}$$

$$S_{a1} = H^2 \cdot \gamma_{soil} \cdot K_a / 2 = 22,00 \text{ kN} \quad \text{Horizontal force from active earth pressure}$$

$$h_{a1} = H / 3 = 0,667 \text{ m} \quad \text{Force arm of active earth pressure}$$

$$\gamma_{a1} = 1,25 \text{ [-]} \quad \text{Load factor for dead load (ultimate limit state)}$$

$$M_{Sd} = \gamma_{ah} \cdot S_{ah} \cdot h_{ah} + \gamma_{a1} \cdot S_{a1} \cdot h_{a1} = 18,33 \text{ kNm} \quad \text{Design bending moment}$$

#### Fiber concrete structure analysis

$$b = 1,000 \text{ m} \quad \text{Width of a cross-section}$$

$$h = 0,250 \text{ m} \quad \text{Height of a cross-section}$$

$$f_{ck} = 25,00 \text{ MPa} \quad \text{Characteristic compressive cylinder strength of plain concrete}$$

$$f_{ct,f} = 3,000 \text{ MPa} \quad \text{Characteristic flexural tensile strength of plain concrete}$$

$$\phi = 0,60 \quad \text{Capacity reduction factor}$$

#### Elastoplastic concrete properties

$$m_f = 2,50 \text{ kg/m}^3 \quad \text{Dosage of plastic fibres per m}^3 \text{ (max. 7,5 kg)}$$

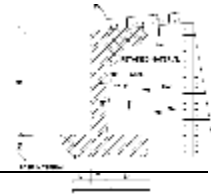
$$f_{fct,f} = 3,356 \text{ MPa} \quad \text{Characteristic flexural tensile strength of fiberconcrete}$$

$$I_y = b \cdot h^3 / 12 = 0,001302 \text{ m}^4 \quad \text{Second moment of area of the cross-section}$$

$$M_{uo} = 1,2 \cdot f_{fct,f} \cdot I_y / (h / 2) \cdot \Phi = 25,172 \text{ kNm} \quad \text{Design strength in bending}$$

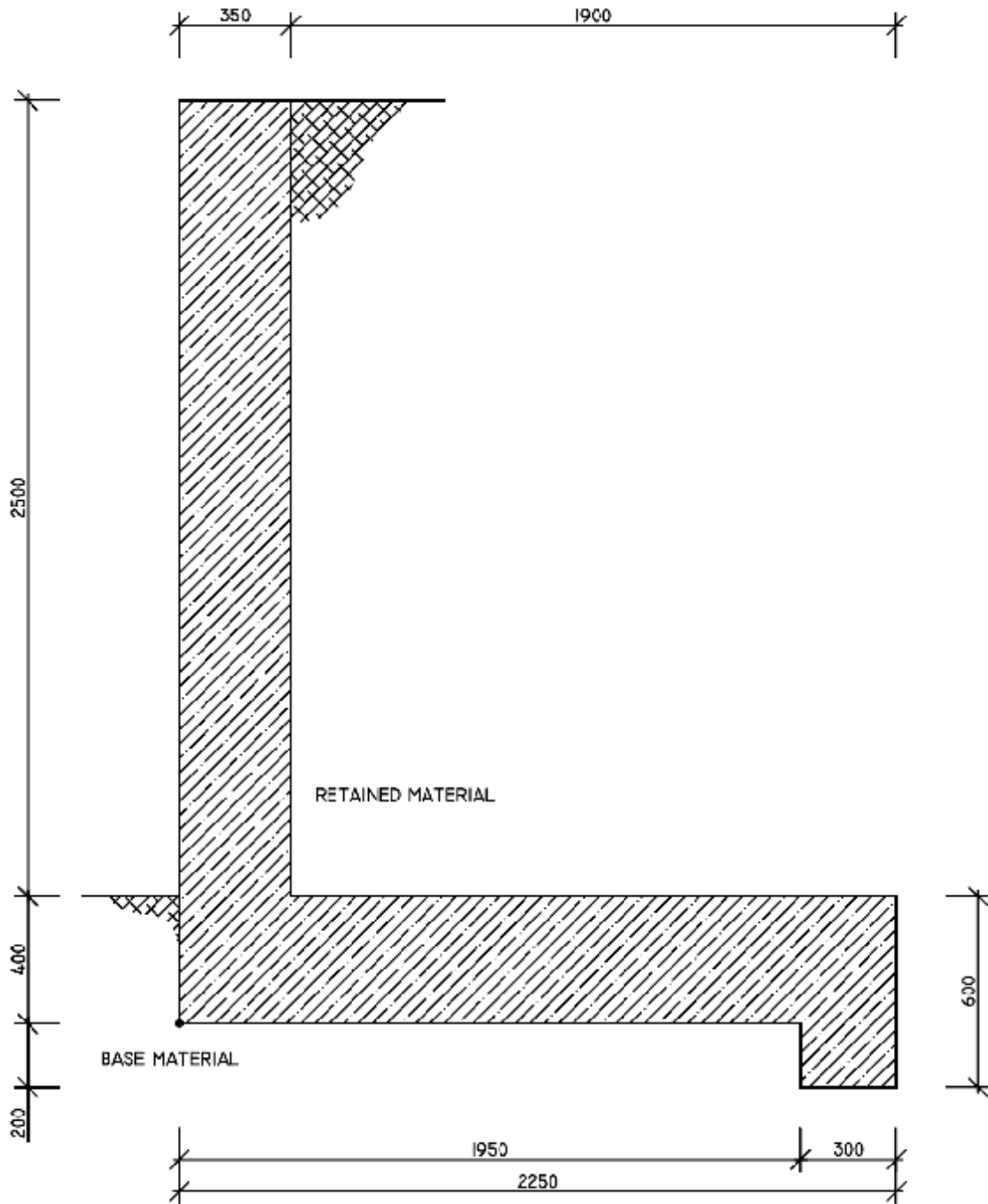
$$M_{uo} = 25,17 \text{ kNm} > M_{Sd} = 18,33 \text{ kNm} \quad \text{OK}$$

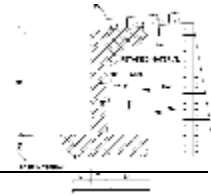




## 8. RETAINING WALL ANALYSIS (0mm - 2500mm HIGH)

### 8.1 Retaining wall model





## 8.2 Retaining wall model

### RETAINING WAL PROPERTIES

#### Retaining wall dimensions

- »  $H = 2,500$  m      *Height of retaining wall stem*
- »  $H_b = 0,400$  m      *Height of retaining wall base*
- »  $h_{\text{soil}} = 0,600$  m      *Height of soil in front of the retaining wall*
- »  $l_t = 0,000$  m      *Length of toe*
- »  $t = 0,350$  m      *Retaining wall thickness*
- »  $l_h = 1,900$  m      *Length of heel*
- »  $\alpha = 0^\circ$       *Angle of rear face of wall*

#### Extra load acting on the ground surface

- »  $f_a = 0,00$  kN/m<sup>2</sup>      *Surcharge load on plan*
- »  $H_{\text{eqv}} = f_a / \gamma_{\text{soil}} = 0,000$  m      *Equivalent height of soil*

#### Retained soil material

- »  $\gamma_{\text{soil}} = 21,00$  kN/m<sup>3</sup>      *Density of soil*
- »  $\varphi_{\text{ef}} = 18,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85$  [-]      *Material strength uncertainty factor*
- »  $\varphi' = 15,44^\circ$       *Design internal friction angle*
- »  $\sigma_{\text{Rd}} = 100$  kPa      *Allowable ultimate bearing pressure*
- »  $\beta = 0^\circ$       *Angle of soil surface behind wall*
- »  $\delta = 10^\circ$       *Angle of base friction*

*The typical soil of this properties is claysoil.*

#### Base soil material

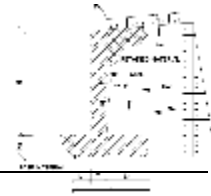
- »  $\gamma_{\text{soil}} = 19,00$  kN/m<sup>3</sup>      *Density of soil*
- »  $\varphi_{\text{ef}} = 35,00^\circ$       *Effective internal friction angle*
- »  $\phi_\varphi = 0,85$  [-]      *Material strength uncertainty factor*
- »  $\varphi' = 30,76^\circ$       *Design internal friction angle*
- »  $\sigma_{\text{Rd}} = 200$  kPa      *Allowable ultimate bearing pressure*
- »  $\delta = 21^\circ$       *Angle of base friction*

*The typical soil of this properties is gravelsoil and sand soil.*

## SOFTWARE ANALYSIS OF RETAINING WALLS

### Analysis of retaining walls of

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#### Concrete

» Concrete: C25/30

$f_{ck} = 25,00$  MPa *Characteristic compressive cylinder strength of plain concrete*

$f_{ct,f} = 3,000$  MPa *Characteristic flexural tensile strength of plain concrete*

»  $\gamma_{con} = 25,00$  kN/m<sup>3</sup> *Density of concrete*

#### Earth pressure factors

$$K_a = \cos^2(\varphi' - \alpha) / [\cos^2(\alpha) \cdot \cos(\alpha + \delta) \cdot (1 + (\sin(\varphi' + \delta) \cdot \sin(\varphi' - \beta)) / (\cos(\alpha + \delta) \cdot \cos(\alpha - \beta)))^{0,5}]^2$$

$K_a = 0,52$  [-] *Active earth pressure factor*

$$K_p = [\sin(90 - \varphi')]^2 / \{\sin(90 - \delta) \cdot [1 - ((\sin(\varphi' + \delta) \cdot \sin(\varphi') / \sin(90 + \delta))^{0,5}]^2\}$$

$K_p = 6,53$  [-] *Passive earth pressure factor*

#### A/ STABILITY ANALYSIS - OVERTURNING

$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000$  kN *Effective value of horizontal surcharge force*

$h_{ak} = (H_b + H) / 2 = 1,450$  m *Force arm of extra surcharge on plan*

$\gamma_{ak} = 1,50$  [-] *Stability load factor for overturning live load*

$S_{a1} = (H_b + H)^2 \cdot \gamma_{soil} \cdot K_a / 2 = 46,3$  kN *Effective value of horizontal active earth press*

$h_{a1} = (H_b + H) / 3 = 0,967$  m *Force arm of active earth pressure*

$\gamma_{a1} = 1,25$  [-] *Stability load factor for overturning dead load*

$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 44,38$  kN *Effective vertical force of concrete R*

$h_{con} = [(l_t + t + l_h)^2 \cdot H_b / 2 + H \cdot t \cdot (l_t + t / 2)] / [(l_t + t + l_h) \cdot H_b + H \cdot t] = 0,657$  m *F*

$\gamma_{con} = 0,90$  [-] *Stability load factor for restoring dead load*

$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 99,75$  kN *Effective vertical force of backfill*

$h_{soil} = l_t + t + l_h / 3 = 0,983$  m *Force arm of backfill*

$\gamma_{soil} = 0,90$  [-] *Stability load factor for restoring dead load*

$M_{over} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 55,89$  kNm *Overturning moment*

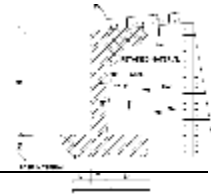
$M_{rest} = G_{con} \cdot h_{con} \cdot \gamma_{con} + G_{soil} \cdot h_{soil} \cdot \gamma_{soil} = 114,5$  kNm *Restoring moment*

$M_{rest} = 114,5$  kNm >  $M_{over} = 55,89$  kNm OK

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of

certain height made of elastoplastic concrete



### B/ ANALYSIS OF STABILITY AGAINST SLIDING

$$S_{ak} = f_a \cdot K_a \cdot (H_b + H) = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$\gamma_{ak} = 1,50 \text{ [-]} \quad \text{Stability load factor for overturning live load}$$

$$S_{a1} = (H_b + H)^2 \cdot \gamma_{soil} \cdot K_a / 2 = 46,3 \text{ kN} \quad \text{Effective value of horizontal active earth press}$$

$$\gamma_{a1} = 1,25 \text{ [-]} \quad \text{Stability load factor for overturning dead load}$$

$$S_{a2} = H_{soil}^2 \cdot \gamma_{soil} \cdot K_p / 2 = 24,7 \text{ kN} \quad \text{Effective value of horizontal passive earth pressure}$$

$$\gamma_{a2} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 44,38 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{con} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 99,75 \text{ kN} \quad \text{Effective vertical force of backfill}$$

$$\gamma_{soil} = 0,90 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$F_{slid} = S_{ak} \cdot \gamma_{ak} + S_{a1} \cdot \gamma_{a1} = 57,81 \text{ kN} \quad \text{Sliding force}$$

$$F_{rest} = \gamma_{a2} \cdot S_{a2} + (G_{con} \cdot \gamma_{con} + G_{soil} \cdot \gamma_{soil}) \cdot \text{tg } \delta = 70,75 \text{ kN} \quad \text{Resistance force}$$

$$F_{rest} = 70,75 \text{ kN} > F_{slid} = 57,81 \text{ kN} \quad \text{OK}$$

### C/ SOIL BEARING CAPACITY ANALYSIS

$$M_{over} = S_a \cdot h_a \cdot \gamma_{ak} + S_{a1} \cdot h_{a1} \cdot \gamma_{a1} = 55,89 \text{ kNm} \quad \text{Overturning moment}$$

$$G_{con} = [(l_t + t + l_h) \cdot H_b + H \cdot t] \cdot \gamma_{con} = 44,38 \text{ kN} \quad \text{Effective vertical force of concrete R}$$

$$\gamma_{con} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$G_{soil} = l_h \cdot H \cdot \gamma_{soil} = 99,75 \text{ kN} \quad \text{Effective vertical force of backfill}$$

$$\gamma_{soil} = 1,25 \text{ [-]} \quad \text{Stability load factor for restoring dead load}$$

$$e = M_{over} / (\gamma_{con} \cdot G_{con} + \gamma_{soil} \cdot G_{soil}) = 0,310 \text{ m} \quad \text{Total force eccentricity}$$

$$e' = (l_t + t + l_h) / 2 - (G_{con} \cdot h_{con} + G_{soil} \cdot h_{soil}) / (G_{con} + G_{soil}) = 0,242 \text{ m}$$

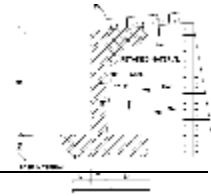
$$b_{eff} = [l_t + t + l_h - 2 \cdot (e + e')] = 1,145 \text{ m} \quad \text{Load effective width}$$

$$\sigma = (1,25 \cdot G_{con} + 1,25 \cdot G_{soil}) / b_{eff} = 157,33 \text{ kPa} \quad \text{Maximum stress in soil}$$

$$\sigma_{Rd} = 200,00 \text{ kPa} > \sigma = 157,33 \text{ kPa} \quad \text{OK}$$

## SOFTWARE ANALYSIS OF RETAINING WALLS

Analysis of retaining walls of  
certain height made of elastoplastic concrete



### D/ ULTIMATE LIMIT STATE OF RETAINING WALL

#### Internal force analysis

$$S_{ah} = f_a \cdot K_a \cdot H = 0,000 \text{ kN} \quad \text{Effective value of horizontal surcharge force}$$

$$h_{ah} = H / 2 = 1,250 \text{ m} \quad \text{Force arm of horizontal surcharge force}$$

$$\gamma_{ah} = 1,50 \text{ [-]} \quad \text{Load factor for live load (ultimate limit state)}$$

$$S_{a1} = H^2 \cdot \gamma_{soil} \cdot K_a / 2 = 34,37 \text{ kN} \quad \text{Horizontal force from active earth pressure}$$

$$h_{a1} = H / 3 = 0,833 \text{ m} \quad \text{Force arm of active earth pressure}$$

$$\gamma_{a1} = 1,25 \text{ [-]} \quad \text{Load factor for dead load (ultimate limit state)}$$

$$M_{Sd} = \gamma_{ah} \cdot S_{ah} \cdot h_{ah} + \gamma_{a1} \cdot S_{a1} \cdot h_{a1} = 35,80 \text{ kNm} \quad \text{Design bending moment}$$

#### Fiber concrete structure analysis

$$b = 1,000 \text{ m} \quad \text{Width of a cross-section}$$

$$h = 0,350 \text{ m} \quad \text{Height of a cross-section}$$

$$f_{ck} = 25,00 \text{ MPa} \quad \text{Characteristic compressive cylinder strength of plain concrete}$$

$$f_{ct,f} = 3,000 \text{ MPa} \quad \text{Characteristic flexural tensile strength of plain concrete}$$

$$\phi = 0,60 \quad \text{Capacity reduction factor}$$

#### Elastoplastic concrete properties

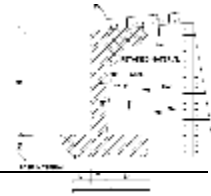
$$m_f = 2,50 \text{ kg/m}^3 \quad \text{Dosage of plastic fibres per m}^3 \text{ (max. 7,5 kg)}$$

$$f_{fct,f} = 3,356 \text{ MPa} \quad \text{Characteristic flexural tensile strength of fiberconcrete}$$

$$I_y = b \cdot h^3 / 12 = 0,003573 \text{ m}^4 \quad \text{Second moment of area of the cross-section}$$

$$M_{uo} = 1,2 \cdot f_{fct,f} \cdot I_y / (h / 2) \cdot \Phi = 49,337 \text{ kNm} \quad \text{Design strength in bending}$$

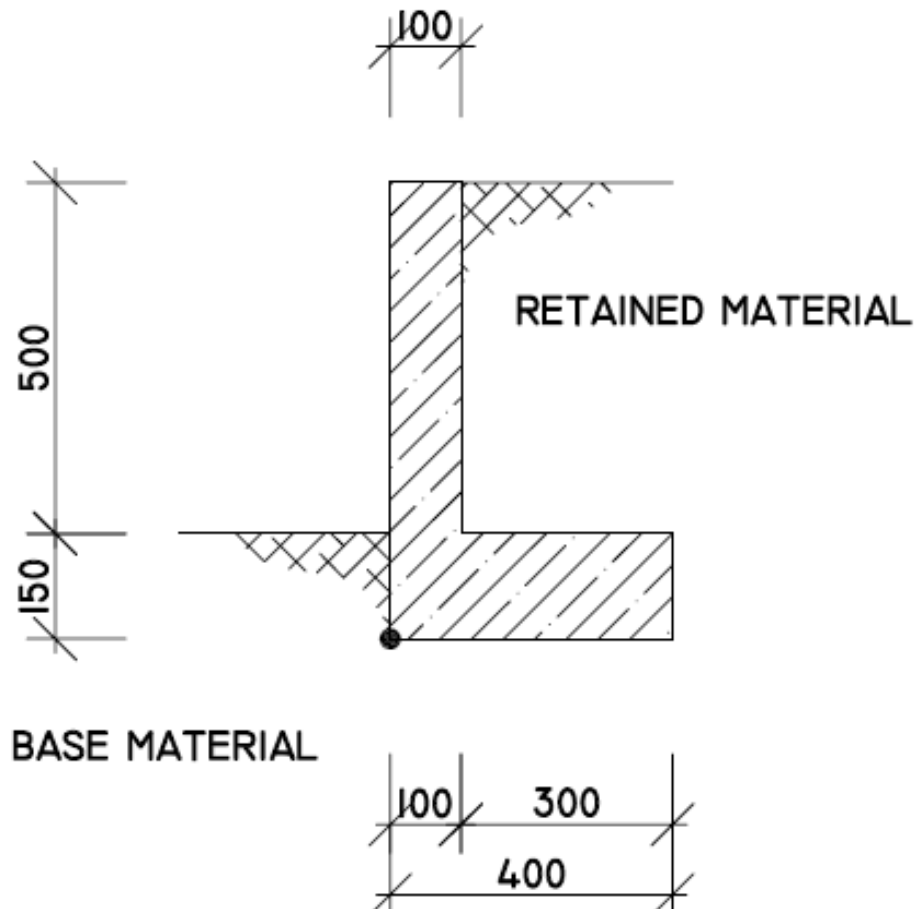
$$M_{uo} = 49,34 \text{ kNm} > M_{Sd} = 35,80 \text{ kNm} \quad \text{OK}$$



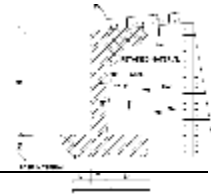
## 9. RESULT SUMMARY

### 9.1 Retaining wall (0mm - 500mm high)

Parameter	Allowable value	Internal force
Stability analysis - overturning	0,89 kNm	0,63 kNm
Stability analysis - sliding	3,38 kN	2,90 kN
Soil bearing capacity	150,00 kPa	44,49 kPa
Ultimate limit state of retaining wall	4,03 kNm	0,29 kNm

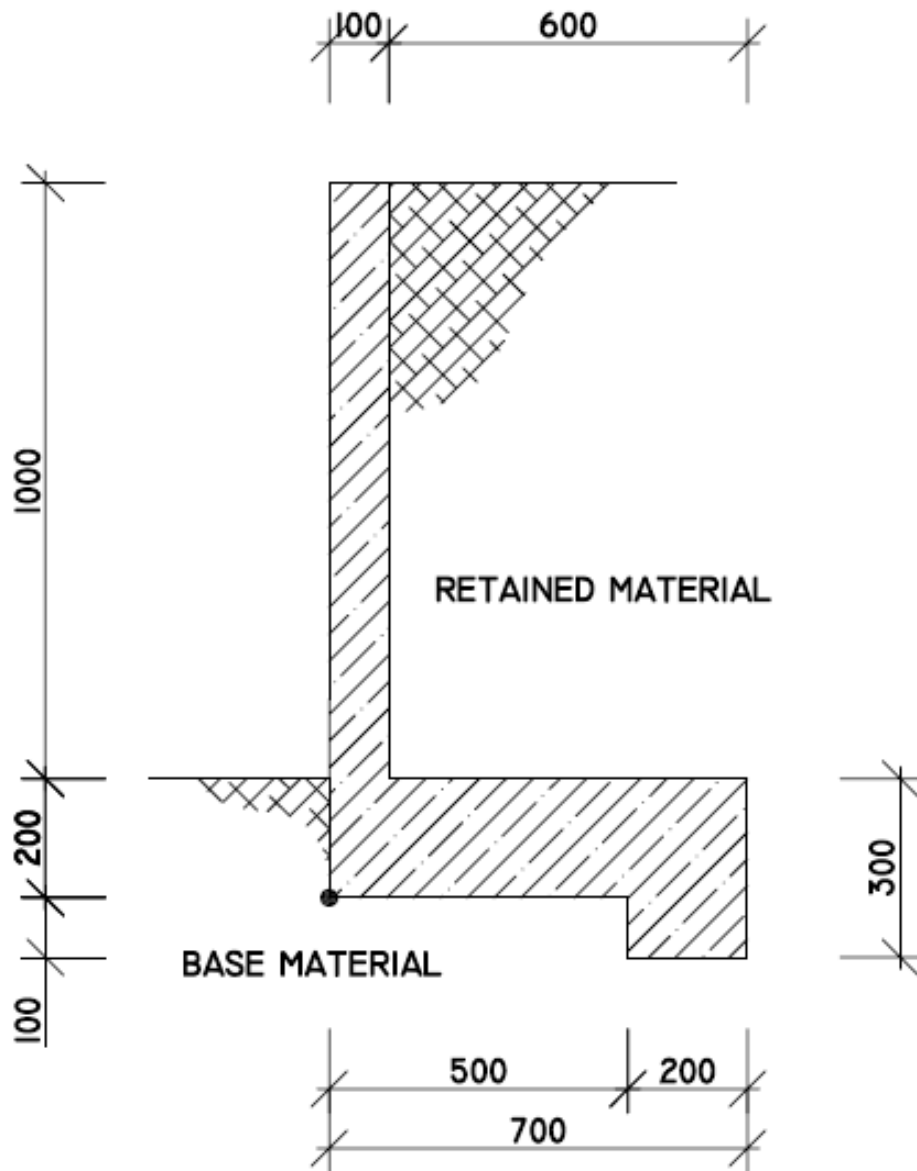


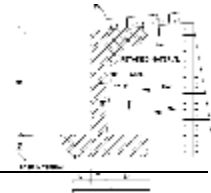
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**9.2 Retaining wall (0mm - 1000mm high)**

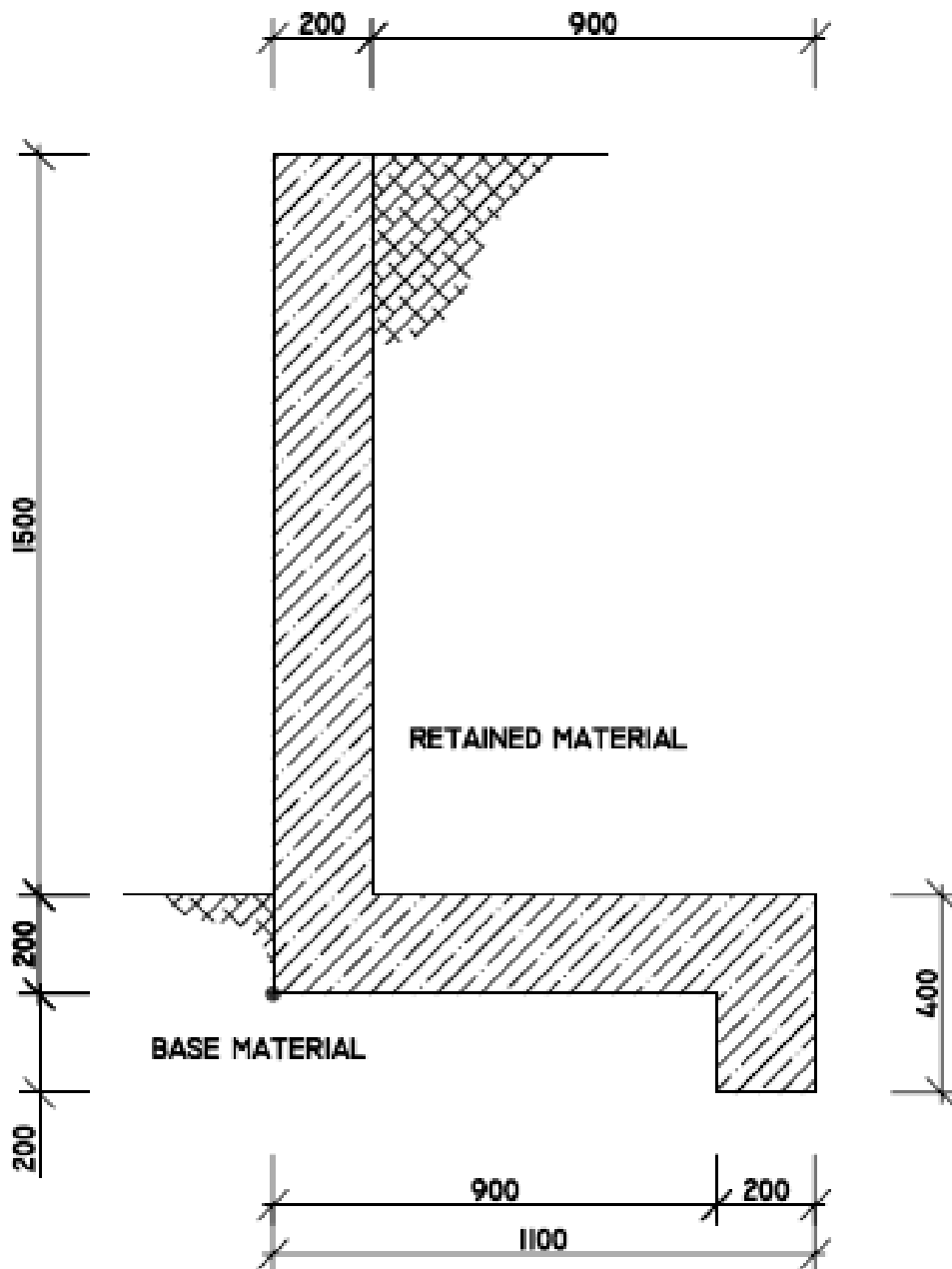
Parameter	Allowable value	Internal force
Stability analysis - overturning	4,62 kNm	3,96 kNm
Stability analysis - sliding	11,82 kN	9,90 kN
Soil bearing capacity	150,00 kPa	110,19 kPa
Ultimate limit state of retaining wall	4,03 kNm	2,29 kNm



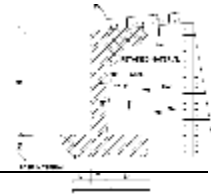


**9.3 Retaining wall (0mm - 1500mm high)**

Parameter	Allowable value	Internal force
Stability analysis - overturning	16,16 kNm	11,26 kNm
Stability analysis - sliding	23,80 kN	19,87 kN
Soil bearing capacity	150,00 kPa	119,49 kPa
Ultimate limit state of retaining wall	16,11 kNm	7,73 kNm

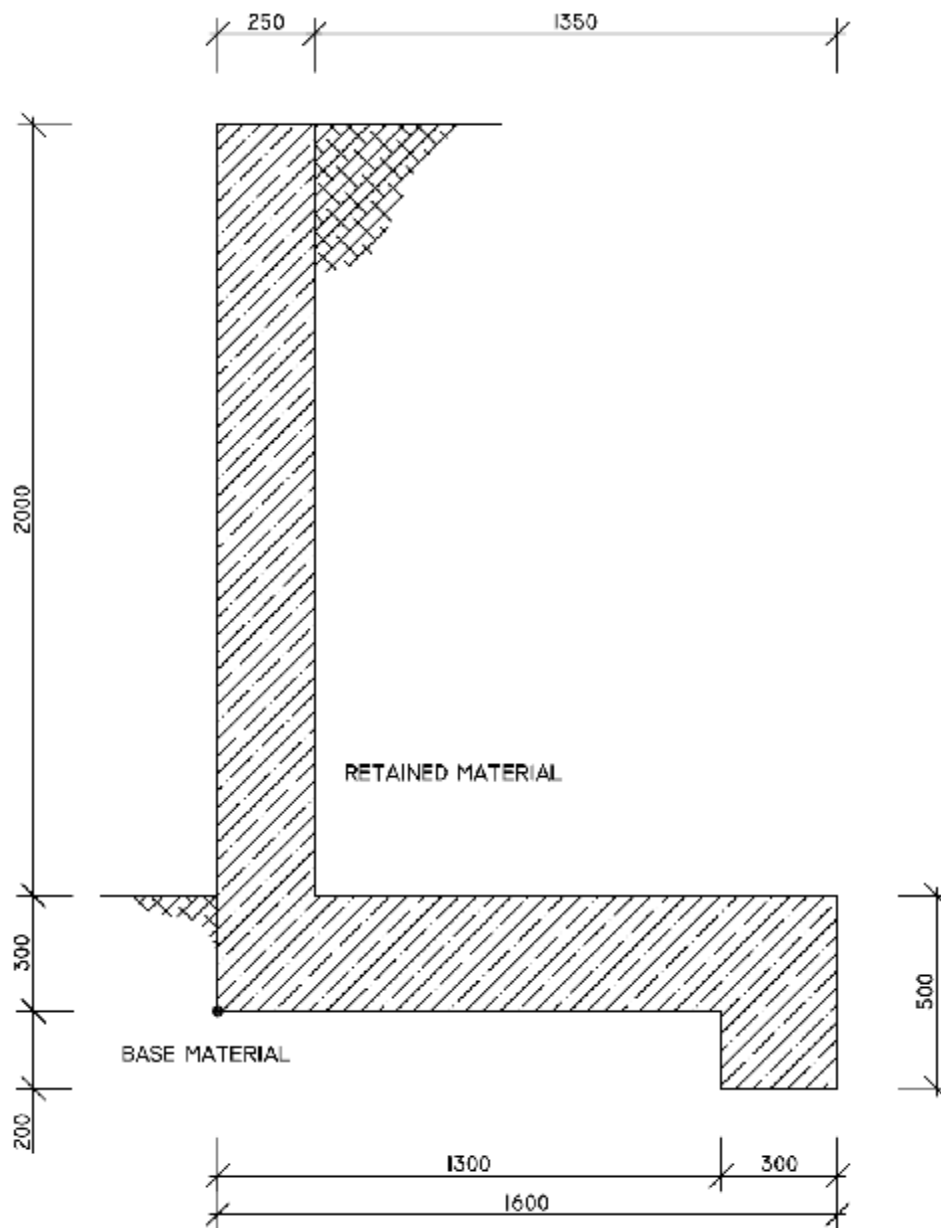






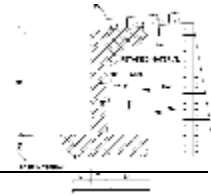
**9.4 Retaining wall (0mm - 2000mm high)**

Parameter	Allowable value	Internal force
Stability analysis - overturning	45,77 kNm	27,88 kNm
Stability analysis - sliding	42,77 kN	36,37 kN
Soil bearing capacity	150,00 kPa	144,35 kPa
Ultimate limit state of retaining wall	25,17 kNm	18,33 kNm



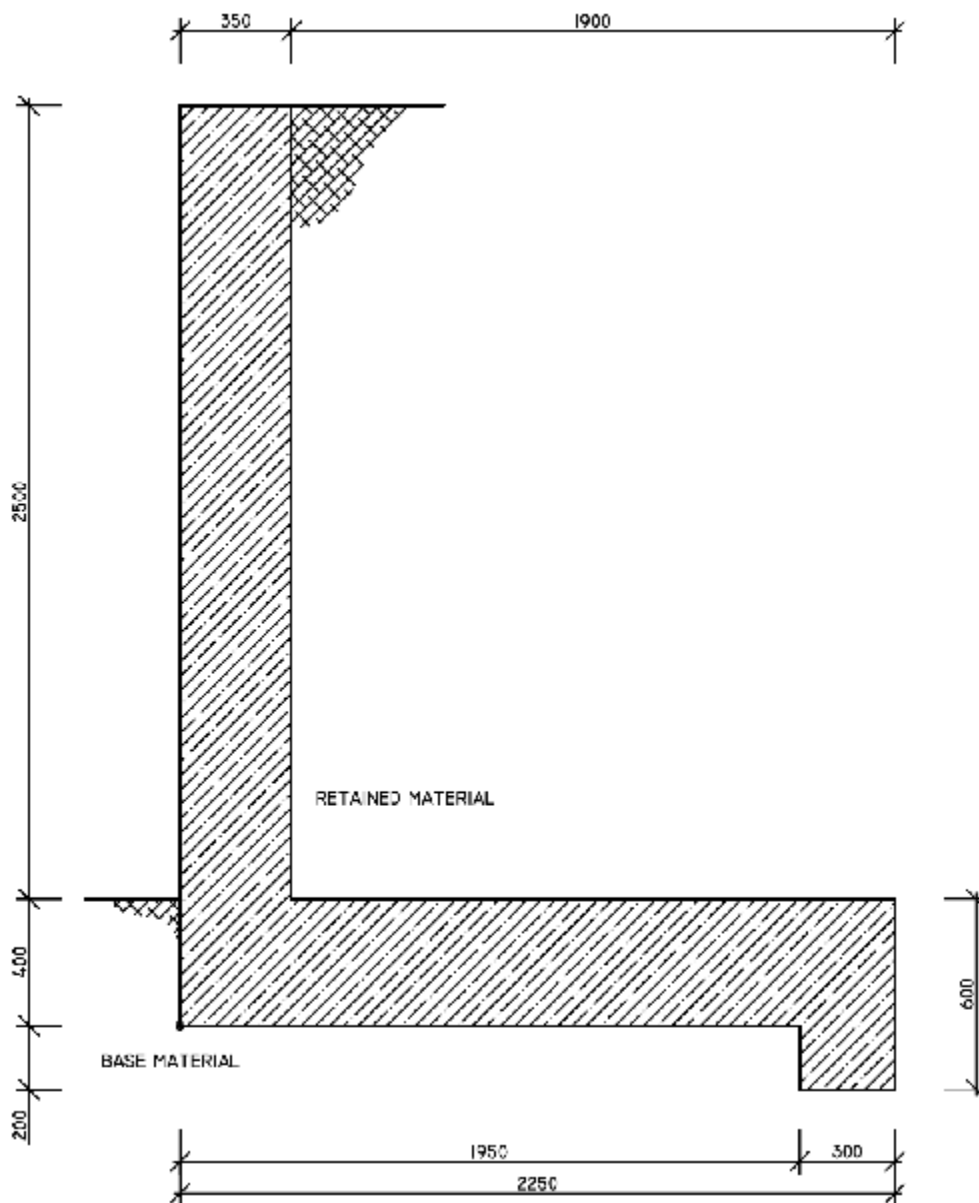
# SOFTWARE ANALYSIS OF RETAINING WALLS

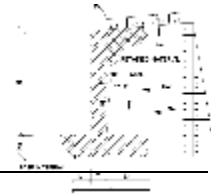
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## 9.5 Retaining wall (0mm - 2500mm high)

Parameter	Allowable value	Internal force
Stability analysis - overturning	114,51 kNm	55,89 kNm
Stability analysis - sliding	70,75 kN	57,81 kN
Soil bearing capacity	200,00 kPa	157,33 kPa
Ultimate limit state of retaining wall	49,34 kNm	35,80 kNm





### 10. CONCLUSION

The analysis in the report shows a possible use of elastoplastic concrete for retaining walls of the certain dimensions. The major issues of the 0 - 2,5m high retaining walls are a stability of a structure. The structure stability depends on a shape of a retaining wall, load and material properties of retained and base material. Load used for the analysis is only the load from soil with no surcharge load on plan or water pressure load.

However the internal forces such as a bending moment does not reach big values. Regarding to that fact elastaoplastic concrete can be efficiently used for the retaining walls described in the report. The location with the maximum bending moment is between a retaining wall steam and a retaining wall base. Based on a practical process of a retaining wall build-up it is still recommended to use starter bars to transfer all the internal forces between these two parts of a retaining wall unless the whole retaining wall is being concreted at one go. That means if a retaining wall could be concreted at one go (without a construction joint), there is no extra reinforcement required. **According to the retaining wall analysis I recommend to use elastoplastic concrete (min concrete C25/30, fiber BarChip48, min. dosage 4 kg/m<sup>3</sup>) for the retaining walls described in the report.**

Retaining walls from elastoplastic concrete with different input conditions (different shape, high, load water pressure, surcharge load on plan, material of retained and base material) might satisfied the requirements in accordance with Australian Standards. However, firstly an analyses of that retaining walls with different input conditions are required.